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Math 104

$$1.) y = t^3 - \frac{t^2}{2} - 2t + 4$$

(i) Stationary point

$$y = t^3 - \frac{t^2}{2} - 2t + 4 \quad ; \text{ at stationary point, } \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = 3t^2 - t - 2 = 0$$

$$3t^2 - t - 2 = 0$$

$$(t-1)(3t+2) = 0$$

$$t = 1 \text{ and } t = -\frac{2}{3}$$

the stationary point is at $t = 1$ or $t = -\frac{2}{3}$

(ii) The coordinates of the stationary point

at $t = 1$

$$y = (1)^3 - \frac{(1)^2}{2} - 2(1) + 4 = 1 - \frac{1}{2} - 2 + 4 = \frac{5}{2} \text{ or } 2.5$$

$$(1, 2.5)$$

at $t = -\frac{2}{3}$

$$y = \left(-\frac{2}{3}\right)^3 - \frac{\left(-\frac{2}{3}\right)^2}{2} - 2\left(-\frac{2}{3}\right) + 4 = \frac{-8}{27} - \frac{2}{9} + \frac{4}{3} + 4 = \frac{130}{27} \text{ or } 4.81$$

$$(-0.67, 4.81)$$

\therefore coordinates of the stationary points are $(1, 2.5)$ and $(-0.67, 4.81)$

(iii) Nature of stationary points of the curve

$$\frac{dy}{dx} = 3t^2 - t - 2 = 0 \quad ; \quad \frac{d^2y}{dx^2} = 6t - 1 = 0$$

$$\text{at } t = 1, \quad \frac{d^2y}{dx^2} = 6(1) - 1 = 6 - 1 = 5$$

\therefore the stationary point at $t = 1$ is a

$$\text{at } t = -\frac{2}{3}, \quad \frac{d^2y}{dx^2} = 6\left(-\frac{2}{3}\right) - 1 = -5$$

\therefore the stationary point at $t = -\frac{2}{3}$ is a

$$2) \quad 2y^2 - 5x^4 - 2 - 7y^3 = 0, \text{ find } \frac{dy}{dx}$$

$$\frac{d}{dx} [2y^2] - \frac{d}{dx} [5x^4] - \frac{d}{dx} (2) - \frac{d}{dx} (7y^3) = 0$$

$$4y \frac{dy}{dx} - 20x^3 - 0 - 21y^2 \frac{dy}{dx} = 0$$

$$4y \frac{dy}{dx} - 21y^2 \frac{dy}{dx} = 20x^3$$

$$\frac{dy}{dx} (4y - 21y^2) = 20x^3$$

$$\therefore \frac{dy}{dx} = \frac{20x^3}{(4y - 21y^2)}$$

$$3) \quad 4x^2 + 2xy^3 - 5y^2 = 0 \text{ find } \frac{dy}{dx}$$

$$\frac{d}{dx} (4x^2) + \frac{d}{dx} (2xy^3) - \frac{d}{dx} (5y^2) = 0$$

$$8x + 2 \left[y^3 + 3y^2 x \frac{dy}{dx} \right] - 10y \frac{dy}{dx} = 0$$

$$8x + 2y^3 + 6y^2 x \frac{dy}{dx} - 10y \frac{dy}{dx} = 0$$

$$6y^2 x \frac{dy}{dx} - 10y \frac{dy}{dx} = -8x - 2y^3$$

$$\therefore \frac{dy}{dx} [6y^2 x - 10y] = -8x - 2y^3$$

$$\frac{dy}{dx} = \frac{-8x - 2y^3}{6y^2 x - 10y}$$

$$\text{when } x=1 \text{ and } y=2; \quad \frac{dy}{dx} = \frac{-8(1) - 2(2)^3}{6(2)^2(1) - 10(2)} = \frac{-8 - 16}{24 - 20} = \frac{-24}{4} = -6$$